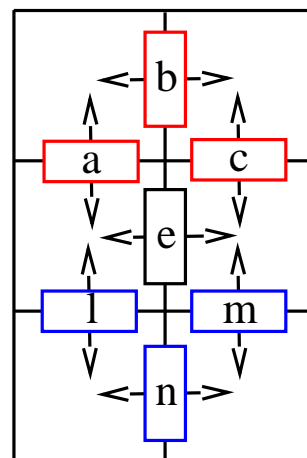
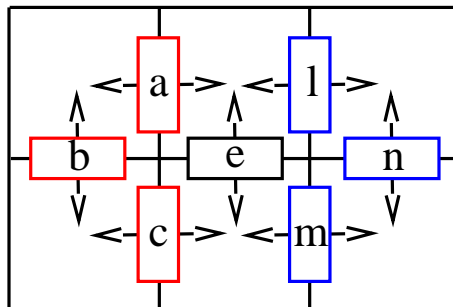




## Edge Relaxation - Linking Contiguous Edges

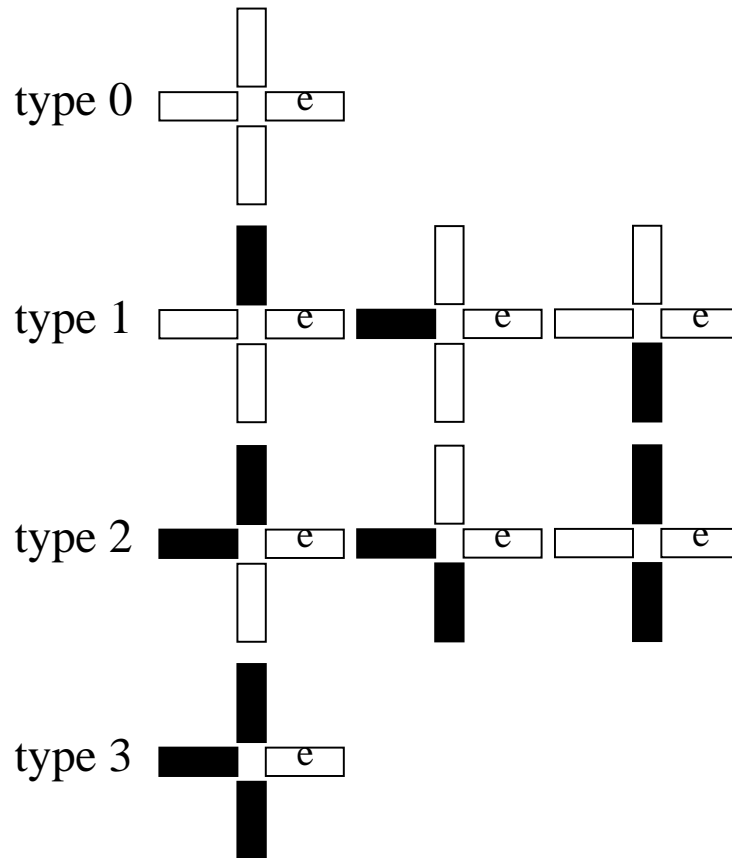
*Any edgelet that is truly part of a larger, continuous contour should have corroborating edgelets representing the continuation of the contour in its neighborhood.*

### Left-Right and Top-Bottom Neighborhoods





## Edge Relaxation - Continuation Types

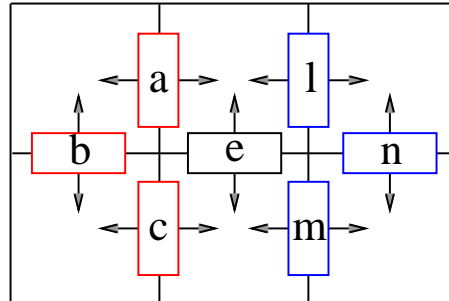


- $q$  - gradient magnitude threshold
- $0 \leq (a, b, c) \leq 1$  - normalized gradient magnitudes,  $a > b > c$ ,
- $m = \max(a, b, c, q)$ .

$conf[0] = (m - a)(m - b)(m - c)$	$a, b, c < q$
$conf[1] = a(m - b)(m - c)$	$a > q; b, c < q$
$conf[2] = ab(m - c)$	$a, b > q; c < q$
$conf[3] = abc$	$a, b, c > q$



# Edge Relaxation - Continuation Heuristics



$$\left. \begin{array}{l} 0 - 0 \\ 0 - 2 \\ 0 - 3 \end{array} \right\} \text{NEGATIVE EVIDENCE} \Rightarrow C^{k+1}(e) = \max(0, C^k(e) - \delta)$$

$$\left. \begin{array}{l} 1 - 1 \\ 1 - 2 \\ 1 - 3 \end{array} \right\} \text{POSITIVE EVIDENCE} \Rightarrow C^{k+1}(e) = \min(1, C^k(e) + \delta)$$

$$\left. \begin{array}{l} 0 - 1 \\ 2 - 2 \\ 2 - 3 \\ 3 - 3 \end{array} \right\} \text{NUETRAL EVIDENCE}$$



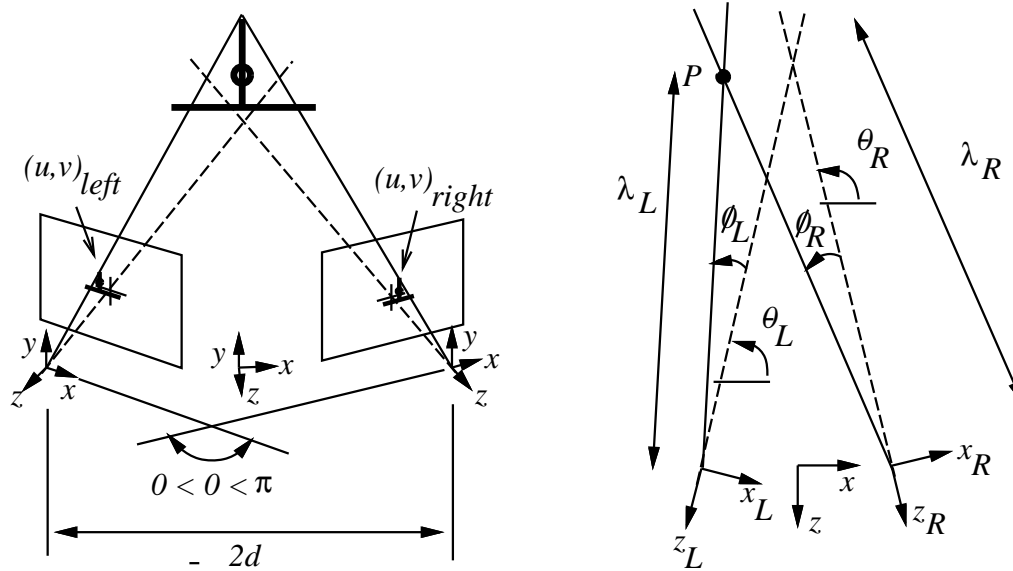
## Hough Transform

*with some knowledge about the shapes of an objects of interest, a so-called “voting” algorithm can be used to identify probable instances of the object*

consider the family of lines described by the slope-intercept form



## Recovering Space - Binocular Stereopsis



$$\lambda_L \cos(\gamma_L) - d = \lambda_R \cos(\gamma_R) + d$$

$$\lambda_L \sin(\gamma_L) = \lambda_R \sin(\gamma_R),$$

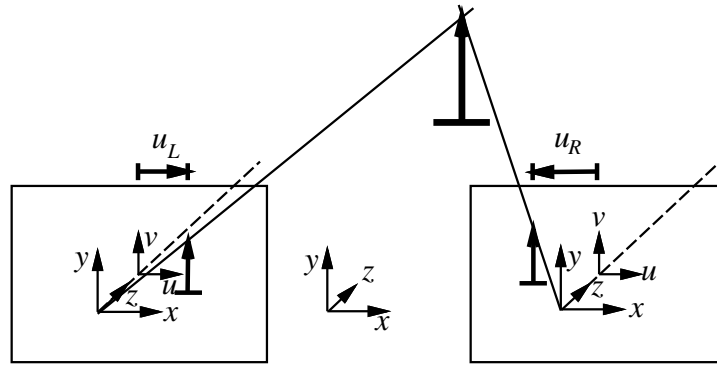
$$\lambda_L = \frac{2d \sin(\gamma_R)}{\sin(\gamma_R - \gamma_L)}$$

$$\lambda_R = \frac{2d \sin(\gamma_L)}{\sin(\gamma_R - \gamma_L)}$$

Depth by **vergence** and **disparity**.



## Depth Encoded as Disparity



Consider this simple binocular configuration. In this geometry, the stereo system encodes depth entirely in terms of disparity. Under these conditions

$$u_L = \frac{f(x - d)}{z} \quad u_R = \frac{f(x + d)}{z}$$

$$zu_R = f(x + d)$$

$$zu_L = f(x - d)$$

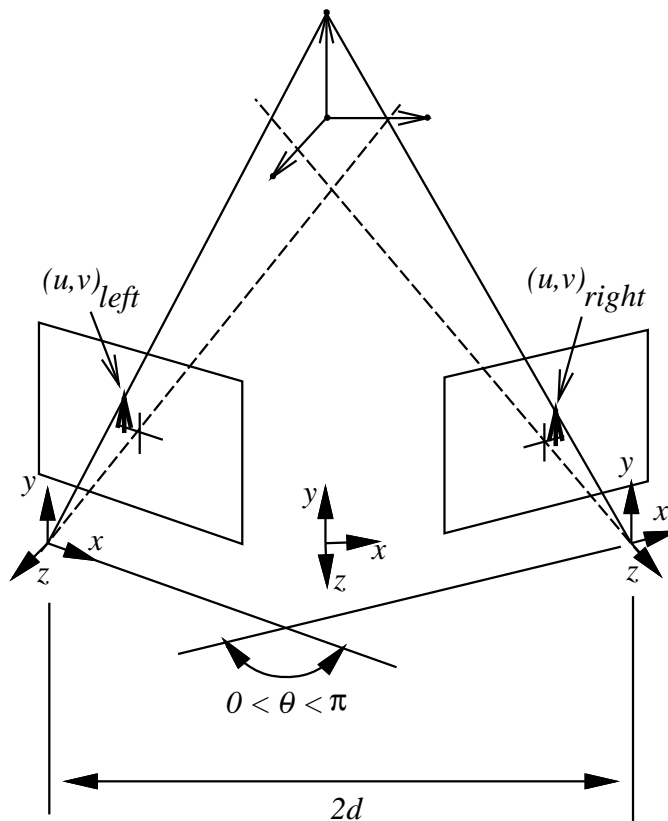
$$z(u_R - u_L) = 2df$$

So by eliminating  $x$ , we may solve directly for  $z$

$$z = \frac{2df}{(u_R - u_L)}$$



# Weak Perspective Affine Transformations



$$\begin{bmatrix} u_L \\ v_L \\ u_R \\ v_R \end{bmatrix} = \begin{bmatrix} A_{00} & A_{01} & A_{02} & A_{03} \\ A_{10} & A_{11} & A_{12} & A_{13} \\ A_{20} & A_{21} & A_{22} & A_{23} \\ A_{30} & A_{31} & A_{32} & A_{33} \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$



## Weak Perspective - cont.

With 4 non-coplanar points, this leads to  
*16 equations in 16 unknowns*

or since;

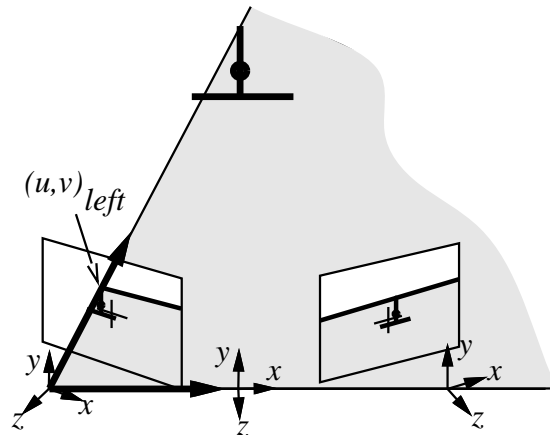
$$\begin{bmatrix} u_L^0 \\ u_L^1 \\ u_L^2 \\ u_L^3 \end{bmatrix} = \begin{bmatrix} A_{00}x^0 & A_{01}y^0 & A_{02}z^0 & A_{03} \\ A_{00}x^1 & A_{01}y^1 & A_{02}z^1 & A_{03} \\ A_{00}x^2 & A_{01}y^2 & A_{02}z^2 & A_{03} \\ A_{00}x^3 & A_{01}y^3 & A_{02}z^3 & A_{03} \end{bmatrix}$$

the solution can be obtained from  $4 \times (4 \text{ equations in } 4 \text{ unknowns})$





## The Epipolar Constraint



**Epipolar plane:** defined by the line joining the focal points of the stereo system and the ray from the left focal point to the image feature of interest.

**Epipolar line:** The intersection of the epipolar plane on the left and right image planes.

Alternatively, the inverse of the  $A$  matrix:

$$\begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} = \begin{bmatrix} A_{00}^{-1} & A_{01}^{-1} & A_{02}^{-1} & A_{03}^{-1} \\ A_{10}^{-1} & A_{11}^{-1} & A_{12}^{-1} & A_{13}^{-1} \\ A_{20}^{-1} & A_{21}^{-1} & A_{22}^{-1} & A_{23}^{-1} \\ A_{30}^{-1} & A_{31}^{-1} & A_{32}^{-1} & A_{33}^{-1} \end{bmatrix} \begin{bmatrix} u_L \\ v_L \\ u_R \\ v_R \end{bmatrix}$$

the forth column yields:

$$1 = A_{03}^{-1}u_L + A_{13}^{-1}v_L + A_{23}^{-1}u_R + A_{33}^{-1}v_R$$



# Vision Programming Environment

## IMAGE structure

```
typedef struct {  
    int width, height, maxval;  
    int *image;  
} IMAGE;
```

## read\_image()

- reads *.pgm* format and converts it to an IMAGE data structure

## remap()

- given IMAGE structure with associated *min* and *max*, remaps image onto 0-255 so that it may be written in *.pgm* format

## write\_image()

- writes IMAGE data structure out to disk in the *.pgm* format



# Stereo Reconstruction Homework

## Image Datasets

multiple images of static scenes from simple polyhedra to complex model train sets taken with a *scientific camera* at the Calibrated Imaging Laboratory at CMU.

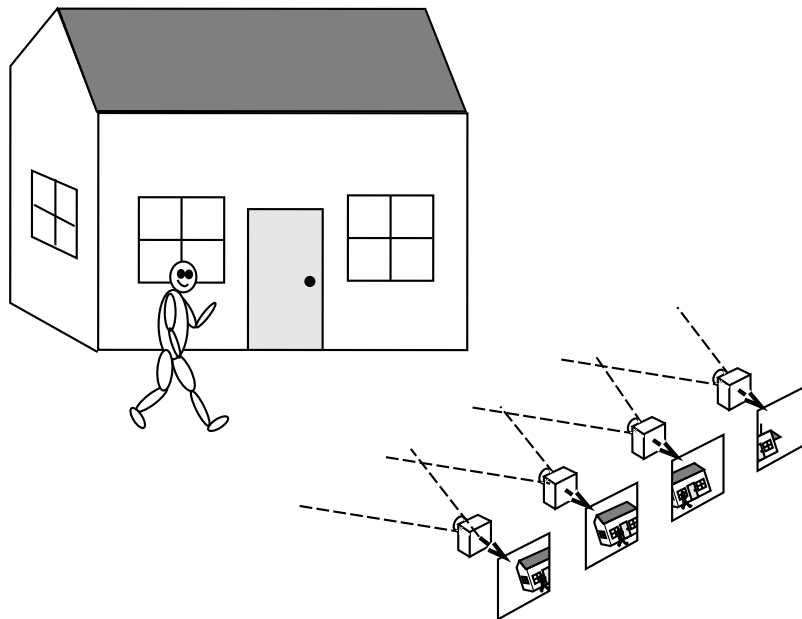
```
ftp ftp.cs.cmu.edu
login: anonymous
passwd: [your email]
cd /usr0/anon/project/cil
binary
dir
get cil-0001.tar
etc.
```

or

<http://www.cs.cmu.edu:8001/usr0/anon/project/cil/html/cil-ster.html>



# Stereo Reconstruction Homework



## Left Image

c-000101.pgm

c-000101.par

## Right Image

c-000103.pgm

c-000103.par

## Parameter Files:

- dimension of a pixel
- pinhole camera effective focal length
- world-camera translation
- world-camera rotation